

Class Thursday 30 March

Repair estimate of  $f_k : f_\mu$  for a plane P wave:

$$s_x = s_y = 0 \quad \text{---||---||---} \rightarrow z$$

$$s_z = A \cos(kz - \omega t)$$

$$\epsilon_{zz} = \partial_z s_z$$

$$d_{xx} = d_{yy} = -\frac{1}{3} \epsilon_{zz}$$

$$d_{zz} = \frac{2}{3} \epsilon_{zz}$$

$$f_k \sim K \epsilon_{zz}^2$$

$$f_\mu \sim 2\mu (d_{xx}^2 + d_{yy}^2 + d_{zz}^2)$$

$$= 2\mu \left( \frac{1}{9} + \frac{1}{9} + \frac{4}{9} \right) \epsilon_{zz}^2$$

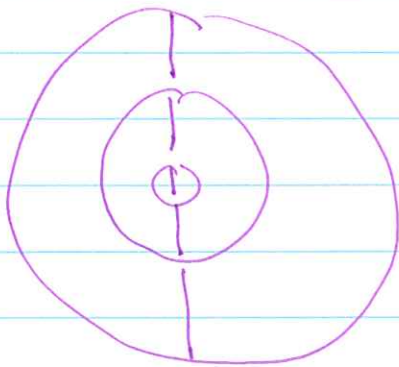
$$= \frac{4}{3}\mu \epsilon_{zz}^2$$

$$f_k : f_\mu = K : \frac{4}{3}\mu \approx \frac{J}{3}\mu : \frac{4}{3}\mu \approx 5:4$$

i.e.  $f_k = \frac{J}{9}$ ,  $f_\mu = \frac{4}{9}$  in Pössner article

~~PPPP mode~~

PKIKP mode



$$f_K = \frac{\frac{5}{9} T_{PCP} + T_{KIK} + \frac{5}{9} T_I}{T_{PKIKP}}$$

$$f_M = \frac{\frac{4}{9} T_{PCP} + \frac{4}{9} T_I}{T_{PKIKP}}$$

$$T_{PCP} \text{ at } \Delta = 0 : 8 \text{ m } 31.5 = 511.5$$

$$T_{PKIKP} \text{ at } \Delta = \pi : 20 \text{ m } 12.5 = 1212.5$$

$$T_I \approx \frac{2434 \text{ km}}{11 \text{ km/s}} \approx \text{~~221~~ 221}$$

$$f_M \approx \frac{\frac{4}{9} (511 + \text{~~221~~})}{1212} = \text{~~0.27~~ 0.27}$$

Then do tsunami modes & atmospheric modes

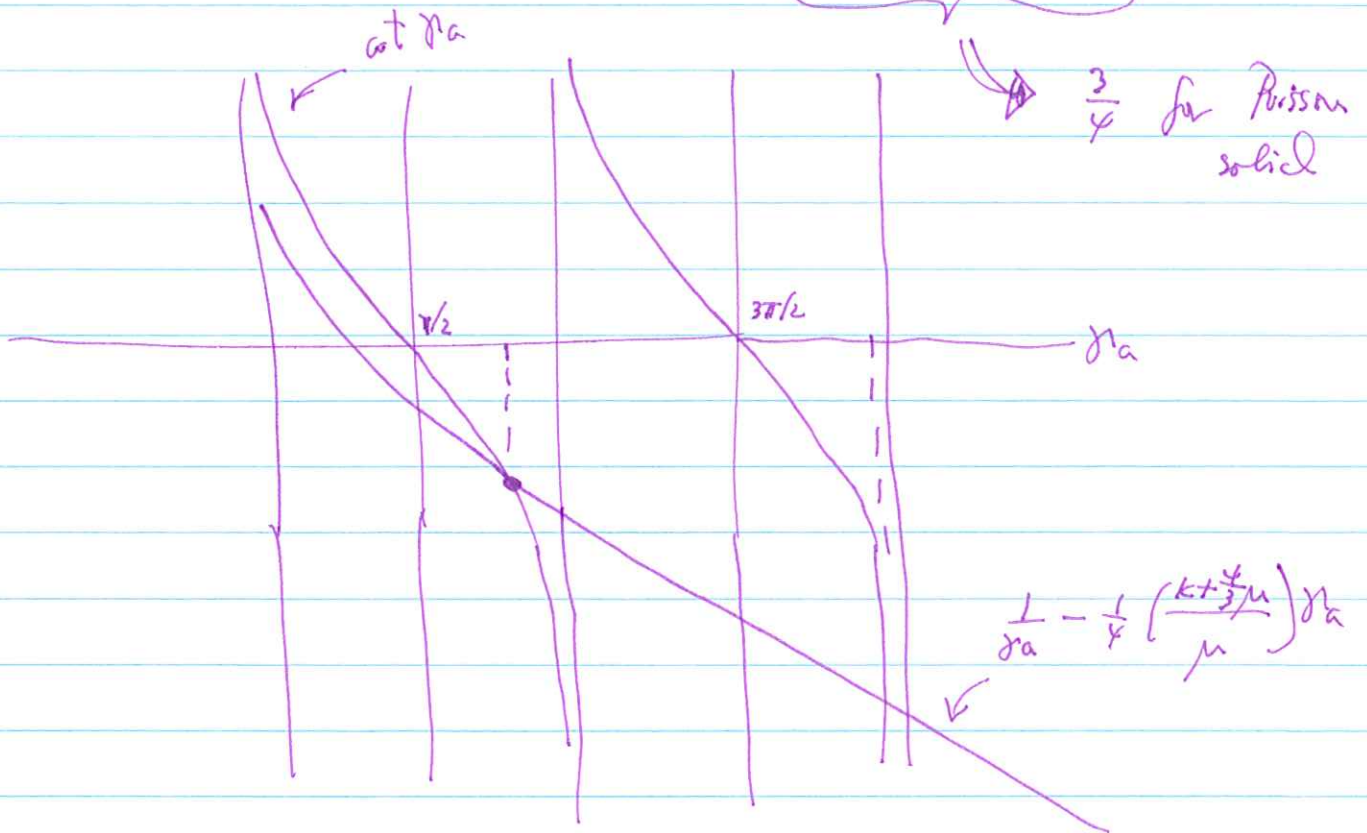
Then do excitation by a transient source Sect 4.1.2

Then do stress glut Ch. 5

Moment tensor representation Sect. 5.4

Radial Mode: homogeneous sphere

$$\cot(\delta a) = \frac{1}{\delta a} - \frac{1}{4} \left( \frac{k + \frac{4}{3}\mu}{\mu} \right) \delta a$$



$$\left. \begin{aligned} \delta_0 a &= 0.82\pi \\ \delta_1 a &= 1.98\pi \end{aligned} \right\} \begin{aligned} &\text{Poisson solid} \\ &\kappa = \frac{5}{3}\mu \end{aligned}$$

Fluid sphere ( $\mu=0$ )  $\cot \delta a = -\infty$

$\Rightarrow$

$$\delta_0 a = (n+1)\pi$$

$$n \omega_0 = \sqrt{\delta_0^2 a^2 - \frac{16}{3} \pi G \rho}$$